

1. (5 points) Evaluate the integral:

$$\int \frac{x^3 - 2\sqrt{x}}{x} dx$$

$$\begin{aligned} &= \int \frac{x^3}{x} - \frac{2x^{1/2}}{x} dx \\ &= \int x^2 - 2x^{-1/2} dx \\ &= \left(\frac{1}{3}x^3 - 4x^{1/2} + C \right) \end{aligned}$$

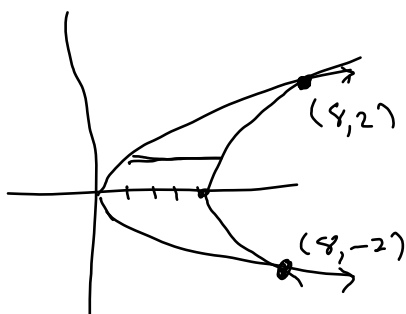
2. (5 points) Evaluate the integral:

$$\int_0^{\sqrt{\pi}} x \cdot \cos(x^2) dx$$

Let $u = x^2$ $x=0 \rightarrow u=0$
 $du = 2x dx$ $x=\sqrt{\pi} \rightarrow u=\pi$

$$\begin{aligned} \int_{u=0}^{u=\pi} x \cos(u) \frac{du}{2x} &= \int_0^{\pi} \frac{1}{2} \cos u du = \frac{1}{2} \sin u \Big|_0^{\pi} = \frac{1}{2} (\sin \pi - \sin 0) \\ &= \boxed{0} \end{aligned}$$

3. (5 points) Find the area of the region bounded by the curves $x = 2y^2$ and $x = 4 + y^2$.



Solve $2y^2 = 4 + y^2$

$$y^2 = 4$$

$$y = \pm 2$$

$$A = \int_{-2}^2 (4 + y^2) - 2y^2 dy$$

$$= \int_{-2}^2 (4 - y^2) dy$$

$$= 2 \int_0^2 (4 - y^2) dy \quad (\text{by symmetry})$$

$$= 2 \left(4y - \frac{y^3}{3} \right) \Big|_0^2 = 2 \left(8 - \frac{8}{3} \right) = \boxed{\frac{32}{3}}$$